

Package ‘nse’

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Title Numerical Standard Errors Computation in R

Description Collection of functions designed to calculate numerical standard error (NSE) of univariate time series as described in Ardia et al. (2018) <[doi:10.1515/jtse-2017-0011](https://doi.org/10.1515/jtse-2017-0011)> and Ardia and Bluteau (2017) <[doi:10.21105/joss.00172](https://doi.org/10.21105/joss.00172)>.

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BugReports <https://github.com/keblu/nse/issues>

URL <https://github.com/keblu/nse>

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Suggests testthat

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nse

nse: Computation of numerical standard errors in R

Description

nse (Ardia and Bluteau, 2017) is an R package for computing the numerical standard error (NSE), an estimate of the standard deviation of a simulation result, if the simulation experiment were to be repeated many times. The package provides a set of wrappers around several R packages, which give access to more than thirty NSE estimators, including batch means estimators (Geyer, 1992, Section 3.2), initial sequence estimators Geyer (1992, Equation 3.3), spectrum at zero estimators (Heidelberger and Welch, 1981), heteroskedasticity and autocorrelation consistent (HAC) kernel estimators (Newey and West, 1987; Andrews, 1991; Andrews and Monahan, 1992; Newey and West, 1994; Hirukawa, 2010), and bootstrap estimators Politis and Romano (1992, 1994); Politis and White (2004). The full set of estimators is described in Ardia et al. (2018).

Functions

- `nse.geyer`: Geyer NSE estimator.
- `nse.spec0`: Spectral density at zero NSE estimator.
- `nse.nw`: Newey-West NSE estimator.
- `nse.andrews`: Andrews NSE estimator.
- `nse.hiruk`: Hirukawa NSE estimator.
- `nse.boot`: Bootstrap NSE estimator.

Note

Functions rely on the packages `coda`, `mcmc`, `mcmcse`, `np`, and `sandwich`.

Please cite the package in publications. Use `citation("nse")`.

Author(s)

David Ardia and Keven Bluteau

References

- Andrews, D.W.K. (1991). Heteroskedasticity and autocorrelation consistent covariance matrix estimation. *Econometrica* **59**(3), 817-858.
- Andrews, D.W.K, Monahan, J.C. (1992). An improved heteroskedasticity and autocorrelation consistent covariance matrix estimator. *Econometrica* **60**(4), 953-966.
- Ardia, D., Bluteau, K., Hoogerheide, L. (2018). Methods for computing numerical standard errors: Review and application to Value-at-Risk estimation. *Journal of Time Series Econometrics* **10**(2), 1-9. doi:10.1515/jtse20170011 doi:10.2139/ssrn.2741587
- Ardia, D., Bluteau, K. (2017). nse: Computation of numerical standard errors in R. *Journal of Open Source Software* **10**(2). doi:10.21105/joss.00172

- Geyer, C.J. (1992). Practical Markov chain Monte Carlo. *Statistical Science* **7**(4), 473-483.
- Heidelberger, P., Welch, Peter D. (1981). A spectral method for confidence interval generation and run length control in simulations. *Communications of the ACM* **24**(4), 233-245.
- Hirukawa, M. (2010). A two-stage plug-in bandwidth selection and its implementation for covariance estimation. *Econometric Theory* **26**(3), 710-743.
- Newey, W.K., West, K.D. (1987). A simple, positive semi-definite, heteroskedasticity and autocorrelation-consistent covariance matrix. *Econometrica* **55**(3), 703-708.
- Newey, W.K., West, K.D. (1994). Automatic lag selection in covariance matrix estimation. *Review of Economic Studies* **61**(4), 631-653.
- Politis, D.N., Romano, and J.P. (1992). A circular block-resampling procedure for stationary data. In *Exploring the limits of bootstrap*, John Wiley & Sons, 263-270.
- Politis, D.N., Romano, and J.P. (1994). The stationary bootstrap. *Journal of the American Statistical Association* **89**(428), 1303-1313.
- Politis, D.N., White, H. (2004). Automatic block-length selection for the dependent bootstrap. *Econometric Reviews* **23**(1), 53-70.

See Also

Useful links:

- <https://github.com/keblu/nse>
- Report bugs at <https://github.com/keblu/nse/issues>

nse.andrews

Andrews estimator

Description

Function which calculates the numerical standard error with the kernel based variance estimator by Andrews (1991).

Usage

```
nse.andrews(  
  x,  
  type = c("bartlett", "parzen", "tukey", "qs", "trunc"),  
  lag.prewhite = 0,  
  approx = c("AR(1)", "ARMA(1,1)")  
)
```

Arguments

x	A numeric vector.
type	The type of kernel used among which "bartlett", "parzen", "qs", "trunc" and "tukey". Default is type = "bartlett".
lag.prewHITE	PrewHITE the series before analysis (integer or NULL). When lag.prewHITE = NULL this performs automatic lag selection. Default is lag.prewHITE = 0 that is no prewhitening.
approx	Andrews approximation, either "AR(1)" or "ARMA(1,1)". Default is approx = "AR(1)".

Details

This kernel based variance estimation apply weight to the auto-covariance function with a kernel and sums up the value.

Value

The NSE estimator.

Note

nse.andrews is a wrapper around [lrvAr](#) from the **sandwich** package and uses Andrews (1991) automatic bandwidth estimator. See the documentation of **sandwich** for details.

Author(s)

David Ardia and Keven Bluteau

References

- Andrews, D.W.K. (1991). Heteroskedasticity and autocorrelation consistent covariance matrix estimation. *Econometrica* **59**(3), 817-858.
- Andrews, D.W.K, Monahan, J.C. (1992). An improved heteroskedasticity and autocorrelation consistent covariance matrix estimator. *Econometrica* **60**(4), 953-966.
- Newey, W.K., West, K.D. (1987). A simple, positive semi-definite, heteroskedasticity and autocorrelation consistent covariance matrix. *Econometrica* **55**(3), 703-708.
- Newey, W.K., West, K.D. (1994). Automatic lag selection in covariance matrix estimation. *Review of Economic Studies* **61**(4), 631-653.

Examples

```
## Not run:
n      = 1000
ar     = 0.9
mean  = 1
sd    = 1

set.seed(1234)
```

```
x = c(arima.sim(n = n, list(ar = ar), sd = sd) + mean)

nse.andrews(x = x, type = "parzen", lag.prewHITE = 0)
nse.andrews(x = x, type = "tukey", lag.prewHITE = 1)
nse.andrews(x = x, type = "qs", lag.prewHITE = NULL)

## End(Not run)
```

nse.boot

Bootstrap estimator

Description

Function which calculates the numerical standard error with bootstrap estimator.

Usage

```
nse.boot(x, nb, type = c("stationary", "circular"), b = NULL, lag.prewHITE = 0)
```

Arguments

x	A numeric vector.
nb	The number of bootstrap replications.
type	The bootstrap scheme used, among "stationary" and "circular". Default is type = "stationary".
b	The block length for the block bootstrap. If NULL automatic block length selection. Default is b = NULL.
lag.prewHITE	PrewHITE the series before analysis (integer or NULL). When lag.prewHITE = NULL this performs automatic lag selection. Default is lag.prewHITE = 0 that is no prewhitening.

Value

The NSE estimator.

Note

nse.boot uses [b.star](#) of the **np** package for the optimal block length selection.

Author(s)

David Ardia and Keven Bluteau

References

Politis, D.N., Romano, and J.P. (1992). A circular block-resampling procedure for stationary data. In *Exploring the limits of bootstrap*, John Wiley & Sons, 263-270.

Politis, D.N., Romano, and J.P. (1994). The stationary bootstrap. *Journal of the American Statistical Association* **89**(428), 1303-1313.

Politis, D.N., White, H. (2004). Automatic block-length selection for the dependent bootstrap. *Econometric Reviews* **23**(1), 53-70.

Examples

```
## Not run:
n   = 1000
ar  = 0.9
mean = 1
sd  = 1

set.seed(1234)
x = c(arima.sim(n = n, list(ar = ar), sd = sd) + mean)

set.seed(1234)
nse.boot(x = x, nb = 1000, type = "stationary", b = NULL, lag.prewHITE = 0)
nse.boot(x = x, nb = 1000, type = "circular", b = NULL, lag.prewHITE = NULL)
nse.boot(x = x, nb = 1000, type = "circular", b = 10, lag.prewHITE = NULL)

## End(Not run)
```

nse.cos

Long-run variance estimation using low-frequency cosine series.

Description

Function which calculates the numerical standard error with low-frequency cosine weighted averages of the original serie.

Usage

```
nse.cos(x, q = 12, lag.prewHITE = 0)
```

Arguments

x	A numeric vector.
q	Number of cosine series.
lag.prewHITE	Prewhiten the series before analysis (integer or NULL). When lag.prewHITE = NULL this performs automatic lag selection. Default is lag.prewHITE = 0 that is no prewhitening.

Details

The method estimate the series with a linear regression using cosine low frequency series. It than derived the NSE from the coefficient of the cosine series (Ulrich and Watson, 2017).

Value

The NSE estimator.

Author(s)

David Ardia and Keven Bluteau

References

Muller, Ulrich K., and Mark W. Watson. (2015) Low-frequency econometrics. *National Bureau of Economic Research*, No. w21564.

Examples

```
## Not run:
n   = 1000
ar  = 0.9
mean = 1
sd  = 1
set.seed(1234)
x = c(arima.sim(n = n, list(ar = ar), sd = sd) + mean)

nse.cos(x = x, q = 12, lag.prewhite = 0)
nse.cos(x = x, q = 12, lag.prewhite = NULL)

## End(Not run)
```

nse.geyer

Geyer estimator

Description

Function which calculates the numerical standard error with the method of Geyer (1992).

Usage

```
nse.geyer(
  x,
  type = c("iseq", "bm", "obm", "iseq.bm"),
  nbatch = 30,
  iseq.type = c("pos", "dec", "con")
)
```

Arguments

x	A numeric vector.
type	The type which can be either "iseq", "bm", "obm" or "iseq.bm". See *Details*. Default is type = "iseq".
nbatch	Number of batches when type = "bm" and type = "iseq.bm". Default is nbatch = 30.
iseq.type	Constraints on function: "pos" for nonnegative, "dec" for nonnegative and non-increasing, and "con" for nonnegative, nonincreasing, and convex. Default is iseq.type = "pos".

Details

The type "iseq" gives the positive initial sequence estimator, "bm" is the batch mean estimator, "obm" is the overlapping batch mean estimator and "iseq.bm" is a combination of "iseq" and "bm".

Value

The NSE estimator.

Note

nse.geyer relies on the functions `initseq` from the `mcmc` package and `mcse` from the package `mcmcse`; see the documentation of these packages for more details.

Author(s)

David Ardia and Keven Bluteau

References

Geyer, C.J. (1992). Practical Markov chain Monte Carlo. *Statistical Science* 7(4), 473-483.

Examples

```
## Not run:
n = 1000
ar = 0.9
mean = 1
sd = 1
set.seed(1234)
x = c(arima.sim(n = n, list(ar = ar), sd = sd) + mean)
nse.geyer(x = x, type = "bm", nbatch = 30)
nse.geyer(x = x, type = "obm", nbatch = 30)
nse.geyer(x = x, type = "iseq", iseq.type = "pos")
nse.geyer(x = x, type = "iseq.bm", iseq.type = "con")

## End(Not run)
```

nse.hiruk	<i>Hirukawa estimator</i>
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Description

Function which calculates the numerical standard error with the kernel based variance estimator by Andrews (1991) using Hirukawa (2010) automatic bandwidth estimator.

Usage

```
nse.hiruk(x, type = c("bartlett", "parzen"), lag.prewHITE = 0)
```

Arguments

x	A numeric vector.
type	The type of kernel used among "bartlett" and "parzen". Default is type = "Bartlett".
lag.prewHITE	PrewHITE the series before analysis (integer or NULL). When lag.prewHITE = NULL this performs automatic lag selection. Default is lag.prewHITE = 0 that is no prewhitening.

Value

The NSE estimator.

Note

nse.hiruk is a wrapper around `lrvar` from the **sandwich** package and uses Hirukawa (2010) bandwidth estimator. See the documentation of **sandwich** for details.

Author(s)

David Ardia and Keven Bluteau

References

Hirukawa, M. (2010). A two-stage plug-in bandwidth selection and its implementation for covariance estimation. *Econometric Theory* **26**(3), 710-743.

Examples

```
## Not run:  
n = 1000  
ar = 0.9  
mean = 1  
sd = 1  
  
set.seed(1234)
```

```
x = c(arima.sim(n = n, list(ar = ar), sd = sd) + mean)
nse.hiruk(x = x, type = "parzen", lag.prewHITE = 0)
nse.hiruk(x = x, type = "bartlett", lag.prewHITE = NULL)

## End(Not run)
```

nse.nw

Newey-West estimator

Description

Function which calculates the numerical standard error with the Newey West (1987, 1994) HAC estimator.

Usage

```
nse.nw(x, lag.prewHITE = 0)
```

Arguments

x	A numeric vector
lag.prewHITE	PrewHITE the series before analysis (integer or NULL). When lag.prewHITE = NULL this performs automatic lag selection. Default is lag.prewHITE = 0 that is no prewhitening.

Value

The NSE estimator.

Note

nse.nw is a wrapper around [lrv](#) from the **sandwich** package. See the documentation of **sandwich** for details.

Author(s)

David Ardia and Keven Bluteau

References

Newey, W.K., West, K.D. (1987). A simple, positive semi-definite, heteroskedasticity and autocorrelation-consistent covariance matrix. *Econometrica* **55**(3), .703-708.

Newey, W.K., West, K.D. (1994). Automatic lag selection in covariance matrix estimation. *Review of Economic Studies* **61**(4), .631-653.

Examples

```
## Not run:
n   = 1000
ar  = 0.9
mean = 1
sd  = 1

set.seed(1234)
x = c(arima.sim(n = n, list(ar = ar), sd = sd) + mean)

nse.nw(x = x, lag.prewHITE = 0)
nse.nw(x = x, lag.prewHITE = 1)
nse.nw(x = x, lag.prewHITE = NULL)

## End(Not run)
```

nse.spec0

Spectral density at zero estimator

Description

Function which calculates the numerical standard error with the spectrum at zero estimator.

Usage

```
nse.spec0(
  x,
  type = c("ar", "glm", "daniell", "modified.daniell", "tukey-hanning", "parzen",
    "triweight", "bartlett-priestley", "triangular", "qs"),
  lag.prewHITE = 0,
  welch = FALSE,
  steep = FALSE
)
```

Arguments

x	A numeric vector.
type	Method to use in estimating the spectral density function, among "ar", "glm", "daniell", "modified.daniell", "tukey-hanning", "parzen", "triweight", "bartlett-priestley", "triangular", and "qs". See *Details*. Default is type = "ar".
lag.prewHITE	PrewHITE the series before analysis (integer or NULL). When lag.prewHITE = NULL this performs automatic lag selection. Default is lag.prewHITE = 0 that is no prewhitening.
welch	Use Welch's method (Welsh, 1967) to estimate the spectral density.
steep	Use steep or sharp version of the kernel (Phillips et al., 2006) (only available for type: "qs", "triangular", and "parzen"). lag.prewHITE must be set to 0 to use steep version.

Details

Welsh's method use 50% overlap and 8 sub-samples. The method "ar" estimates the spectral density using an autoregressive model, "glm" using a generalized linear model Heidelberg & Welch (1981), "daniell" uses daniell window from the R kernel function, "modified.daniell" uses daniell window the R kernel function, "tukey-hanning" uses the tukey-hanning window, "parzen" uses the parzen window, "triweight" uses the triweight window, "bartlett-priestley" uses the Bartlett-Priestley window, "triangular" uses the triangular window, and "qs" uses the quadratic-spectral window,

This kernel based variance estimator apply weights to smooth out the spectral density using a kernel and takes the spectral density at frequency zero which is equivalent to the variance of the serie. Bandwidth for the kernel is automatically selected using cross-validatory methods (Hurvich, 1985).

Value

The NSE estimator.

Note

nse.spec0 relies on the packages coda; see the documentation of this package for more details.

Author(s)

David Ardia and Keven Bluteau

References

- Heidelberg, P., Welch, Peter D. (1981). A spectral method for confidence interval generation and run length control in simulations. *Communications of the ACM* **24**(4), 233-245.
- Phillips, P. C., Sun, Y., & Jin, S. (2006). Spectral density estimation and robust hypothesis testing using steep origin kernels without truncation. *International Economic Review*, **47**(3), 837-894.
- Welch, P. D. (1967), The use of Fast Fourier Transform for the estimation of power spectra: A method based on time averaging over short, modified periodograms. *IEEE Transactions on Audio and Electroacoustics*, **AU-15**(2): 70-73,
- Hurvich, C. M. (1985). Data-driven choice of a spectrum estimate: extending the applicability of cross-validation methods. *Journal of the American Statistical Association*, **80**(392), 933-940.

Examples

```
## Not run:
n   = 1000
ar  = 0.9
mean = 1
sd  = 1
set.seed(1234)
x = c(arima.sim(n = n, list(ar = ar), sd = sd) + mean)

nse.spec0(x = x, type = "parzen", lag.prewhite = 0, welch = TRUE, steep = TRUE)

## End(Not run)
```

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